FINALTERM EXAMINATION 2009 (Session - 2)

Calculus & Analytical Geometry-I

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Question No: 1 (Marks: 1) - Please choose one

According to Power-Rule of differentiation, if $f(x) = x^n$ where $f(x) = x^n$ where $f(x) = x^n$ number, then

According to Power-Rule of differentiation, if
$$f(x) = x$$
 where $f(x) = x$ where $f(x) = x$

Question No: 2 (Marks: 1) - Please choose one

If a function g is differentiable at a point x and a function f is differentiable at a point q(x), then the is differentiable at point x.

- ► Composition (f o g)
- ► Quotient (f/q)
- Product (f . g)
- ➤ Sum (f + q)

Question No: 3 (Marks: 1) - Please choose one

$$y = f(g(h(x)))$$

$$u = g(h(x))$$

$$v = h(x) \qquad \frac{dy}{dx} = \underline{\hspace{1cm}}$$
then

dy du dv du dv dx

$$\frac{dy}{du}\frac{du}{dv}\frac{dv}{dx}$$





Question No: 4 (Marks: 1) - Please choose one

If a function f is on a closed interval [a,b], then f has both maximum and minimum value on [a,b].

- Continuous
- ▶ Discontinuous
- ▶ None of these

Question No: 5 (Marks: 1) - Please choose one

$$\int_{a}^{x} \frac{t^2}{2} dt$$

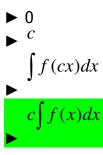
The expression , represents a function of :

- Both x and a

Question No: 6 (Marks: 1) - Please choose one

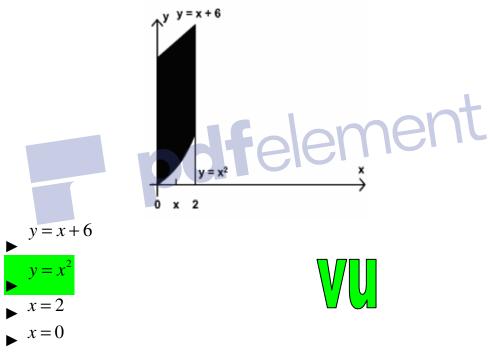
$$\int cf(x)dx = \underline{\hspace{1cm}}$$

if c is a constant



Question No: 7 (Marks: 1) - Please choose one

In the following figure, the area enclosed is bounded below by :



Question No: 8 (Marks: 1) - Please choose one

At what points the two curves: $y = x^2$ and y = x + 6 intersect?

$$x = 0$$
 and $x = 2$

$$x = 0$$
 and $x = 3$

$$x = 2$$
 and $x = 3$

$$x = -2$$
 and $x = 3$

What is the sum of following series?

$$1+2+3+4+_{---}+n$$

$$\frac{n+1}{2}$$

>

$$\frac{(n+1)(n+2)}{2}$$

>

$$n(n+2)$$



$$\frac{n(n+1)}{2}$$

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Question No: 10 (Marks: 1) - Please choose one

If b > 0 then $\frac{d}{dx}[b^x] = \underline{\hspace{1cm}}$

- ▶ (
- xh^{x-}
- ln b
- $b^x \ln b$

Question No: 11 (Marks: 1) - Please choose one

Let S be a solid bounded by two parallel planes perpendicular to the x-axis at x = a and x = b. If , for each x in [a,b], the cross-section area of S perpendicular to the x-axis is A(x), then what is the volume of the solid?

$$V = \int_{a}^{b} A(y) dx$$



$$V = \int_{0}^{A(x)} [b - a] dx$$

$$V = \int_{0}^{A(x)} [b+a]dx$$

▶

Question No: 12 (Marks: 1) - Please choose one

Let the solid generated by the region enclosed between

$$y = \sqrt{x} \quad ; \quad x = 1, x = 4$$

and the x-axis is revolved about the y-axis. Which of the following equation gives the volumes of a solid by cylindrical shells?

$$V = \int_{1}^{4} 2\pi x \sqrt{x} dx$$

$$V = \int_{1}^{4} 2x \sqrt{x} dx$$

$$V = \int_{0}^{4} 2x \sqrt{x} dx$$

$$V = \int_{1}^{4} 2x \sqrt{x} dx$$

▶

Question No: 13 (Marks: 1) - Please choose one

If slope m of a none vertical line is m = 1 then the angle of inclination of the line is

$$\frac{\pi}{2}$$

 $\frac{\pi}{5}$

Question No: 14 (Marks: 1) - Please choose one

The PYTHAGORAS theorem describes the relationship between the sides of

.....

- Right angle triangle
- ► Isoceleous triangle
- ► Equilateral triangle

Question No: 15 (Marks: 1) - Please choose one

If a quantity y depends on another quantity x in such a way that each value of x determines exactly one value of y , we say that y is \dots of x

- ▶ relation
- ▶ function
- not a function
- not a relation

Question No: 16 (Marks: 1) - Please choose one

The graph of the equation $y = x^2 - 4x + 5$ will represent

- ▶ Parabola
- ► Straight line
- ► Two straight lines
- ► Ellipse



Question No: 17 (Marks: 1) - Please choose one

$$\lim_{x \to a} f(x) = \dots \text{where } f(x) = k$$

The

(k is a constant)

Question No: 18 (Marks: 1) - Please choose one

$$\int \frac{1}{x^2 + 2} \ dx$$

Consider the indefinite integral

Let
$$t = x^2 + 2$$

Is the following substitution correct?

$$\int \frac{1}{x^2 + 2} dx = \int \frac{1}{t} dt$$

➤ Yes

Question No: 19 (Marks: 1) - Please choose one



Question No: 20 (Marks: 1) - Please choose one How the series 1-3+5-7+9-11 can be expressed in sigma notation?

$$\sum_{k=0}^{k=5} (-1)^k (2k+1)$$

$$\sum_{k=1}^{k=5} (-1)^k (2k+1)$$

$$\sum_{k=1}^{k=5} (2k+1)$$

$$\sum_{k=1}^{k=5} (2k+1)$$

$$\sum_{k=1}^{k=5} (2k+1)$$

Question No: 21 (Marks: 1) - Please choose one

$$\sum_{k=1}^{n} f(x_{k}^{*}) \Delta x_{k}$$

The sum

is known as:



- ▶ Riemann Sum
- General Sum
- ► Integral Sum
- ▶ Geometric Sum

Question No: 22 (Marks: 1) - Please choose one

$$\sum_{k=1}^{n} f(x_{k}^{*}) \Delta x_{k}$$

What does 'n' represent in the Riemann Sum

- ► No. of Circles
- ► No. of Subintervals
- ► No. of Loops
- ▶ No. of Squares

Question No: 23 (Marks: 1) - Please choose one

If w and v are continuous functions of y on an interval [c, d]

and $w(y) \ge v(y)$ for $c \le y \le d$, then area is bounded by the lines parallel to: :

- ➤ Y-axis
- ➤ X-axis
- Both X-axis and Y-axis

Question No: 24 (Marks: 1) - Please choose one

can be expressed in sigma

$$2(1) + 2(2) + 2(3) + 2(4) + 2(5)$$

How the series notation?

$$\sum_{k=0}^{5} 2k^2$$

$$\sum_{k=1}^{5} 2k^2$$

$$\sum_{k=0}^{5} 2k$$

Question No: 25 (Marks: 1) - Please choose one

$$\sum_{k=1}^{n} \frac{k^3}{2} =$$

$$\frac{n(n+1)}{4}$$



$$\frac{n(n+1)(2n+1)}{12}$$

$$\frac{(n+1)(2n+1)}{\epsilon}$$

Question No: 26 (Marks: 1) - Please choose one

If $a_1 < a_2 < a_3 < < a_n <$, then a sequence $\{a_n\}$

- ► Nondecreasing
- ▶ Decreasing

▶ Nonincreasing

Question No: 27 (Marks: 1) - Please choose one

 $a_1 \ge a_2 \ge a_3 \ge \ge a_n \ge$, then a sequence $\{a_n\}$ is

► Increasing

- ▶ Nondecreasing
- ▶ Decreasing
- Nonincreasing

Question No: 28 (Marks: 1) - Please choose one

If the difference between successive terms $a_{n+1} - a_n > 0$ then the sequence $\{a_n\}$

is known as:

- Increasing
- Decreasing
- ▶ Nondecreasing
- ▶ Nonincreasing

Question No: 29 (Marks: 1) - Please choose one

 $\frac{a_{n+1}}{2} > 1$

if the ratio of successive terms For a sequence is known as:

then the sequence

- Increasing ▶ Decreasing
- ▶ Nondecreasing
- ▶ Nonincreasing



Question No: 30 (Marks: 1) - Please choose one

$$\frac{a_{n+1}}{a_n} \ge 1$$

For a sequence $\{a_n\}$ if the ratio of successive terms then the sequence is known as:

Increasing

- ▶ Decreasing
- ▶ Nondecreasing

► Nonincreasing

Question No: 31 (Marks: 1) - Please choose one

 $f(n) = a_n$ is the nth term of the sequence and f(n) is differentiable and f'(n) > 0 then the sequence will be:

- ▶ Increasing
- ▶ Decreasing
- ▶ Nondecreasing
- ► Nonincreasing

Question No: 32 (Marks: 1) - Please choose one

 $a + ar + ar^2 + ar^3 + ... + ar^{k-1} + ... \quad where \ (a \neq 0)$ If the geometric series |r| < 1

then which of the following is true for the given series?

- Converges
- ▶ Diverges
- ► Gives no information

Question No: 33 (Marks: 1) - Please choose one

 $a+ar+ar^2+ar^3+...+ar^{k-1}+...$ where $(a \neq 0)$ $|r| \geq 1$ If the geometric series , then which of the following is true for the given series?

- ► Converges
- ▶ Diverges
- ▶ Gives no information

Question No: 34 (Marks: 1) - Please choose one

$$\sum_{k=1}^{\infty} u_k$$

$$\sum_{k=1}^{\infty} |u_k|$$

If the series converges but the series does not converge, then



will _____

- ► Converge absolutely
- ▶ Diverge
- ► Converge conditionally



Question No: 35 (Marks: 1) - Please choose one

Let be a series with nonzero terms and suppose that $\rho = \lim_{k \to \infty} \frac{|u_{k+1}|}{|u_k|} > 1$

then which of the following is true?

The series $\frac{\sum |u_k|}{\sum |u_k|}$ converges

- ► The series diverges
- ▶ No conclusion can be drawn.

Question No: 36 (Marks: 1) - Please choose one

Suppose f and g are integrable functions on [a, b] and c is a constant, then

$$\int_{a}^{b} c \left[f(x) + g(x) \right] dx = \underline{\hspace{1cm}}$$

$$\int_{a}^{b} f(cx)dx + \int_{a}^{b} g(cx)dx$$

$$\int_{a}^{b} f(x) dx + \int_{a}^{b} g(x) dx$$



Question No: 37 (Marks: 1) - Please choose one

Which of the following is surface area S generated by revolving the curve y = f(x) between

x = 0 and x = 2 about the x-axis?

$$S = \int_{0}^{2} 2\pi f(x) \sqrt{1 + [f(x)]} dx$$

$$S = \int_{0}^{2} 2\pi f(x) \sqrt{1 + [f'(x)]^{2}} dx$$

$$S = \int_{0}^{2} 2\pi f(x) \sqrt{1 + [f'(x)]} dx$$

$$S = \int_{0}^{2} 2\sqrt{1 + [f'(x)]} dx$$

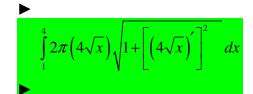
Question No: 38 (Marks: 1) - Please choose one

Which of the following is area of the surface generated by revolving the curve

$$y = 4\sqrt{x}$$
; $1 \le x \le 4$ about the *x*-axis?
$$\int_{0}^{4} 2\pi (4\sqrt{x}) \sqrt{1 + \left[(4\sqrt{x}) \right]^{2}} dx$$

$$\int_{1}^{4} 2\pi \left(4\sqrt{x}\right) \sqrt{1 + \left[\left(4\sqrt{x}\right)'\right]} dx$$

$$\int_{1}^{4} 2\pi + \sqrt{1 + \left[\left(4\sqrt{x} \right)' \right]^{2}} dx$$



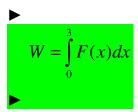
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Question No: 39 (Marks: 1) - Please choose one

Which of the following is the work done W if an object moves in the positive direction along a coordinate line while subject to a force F(x) in the direction of motion over an interval [0,3]?

$$W = \int_{2}^{3} 3x dx$$

$$W = \int_{0}^{3} 3x dx$$



$$W = \int_{3}^{0} F(x) dx$$

Question No: 40 (Marks: 1) - Please choose one

$$\int_{1}^{0} f(x) \ dx = 2 \qquad \int_{0}^{5} f(x) \ dx = 1$$

If

and

then which of the following is value of







Question No: 41 (Marks: 2)

$$\frac{1}{2\sqrt{x}}$$

Derivative of a function is . Find the original function.

Question No: 42 (Marks: 2)

$$\rho = \lim_{k \to +\infty} \sqrt[k]{u_k}$$

is a series with positive terms and ; then write the three cases for the series to be convergent, divergent or none.

Question No: 43 (Marks: 2)

Evaluate the following integral:

$$\int_{1}^{3} \frac{1}{x^2} dx$$

Question No: 44 (Marks: 3)

Use the first fundamental theorem of calculus to evaluate the definite integral:

$$\int_{0}^{2} f(x) dx \quad \text{where} \qquad f(x) = \begin{cases} x^{2} & ; \quad 0 \le x < 1 \\ x^{3} & ; \quad 1 \le x \le 2 \end{cases}$$

Question No: 45 (Marks: 3)

$$\sum_{k=2}^{\infty} (-1)^{k-1} \frac{2^{k-1}}{(k-1)!}$$

Show that the series

converges absolutely.

Question No: 46 (Marks: 3)

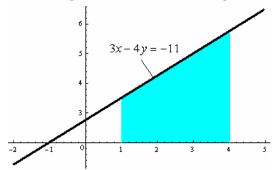
Express the following definite integral as limit of Riemann Sum. (Do not evaluate

the integral)



Question No: 47 (Marks: 5)

Express area of the shaded region as a definite integral.



Question No: 48 (Marks: 5)

How much work is required to wind the chain onto the pulley if a 100-ft length of steel chain weighting

15 lb/ ft. is dangling from a pulley?

Question No: 49 (Marks: 5)

Evaluate the following integral:

$$\int_{1}^{2} \frac{x^2 + \sqrt{x}}{x^2} dx$$

Question No: 50 (Marks: 10)

Use L'Hopital's Rule to evaluate

$$\lim_{x\to 0} (1+\sin x)^{\cot x}$$

This paper is solved by our best knowledge. In the case of any error/correction/suggestion, please contact at gulshanvu@yahoo.com, with reference to the concerned paper's number.

