

MIDTERM EXAMINATION  
Spring 2010  
MTH101- Calculus And Analytical Geometry

Time: 60 min  
Marks: 40

Question No: 1 ( Marks: 1 ) - Please choose one

$$30^{\circ} = \underline{\hspace{2cm}}$$

▶  $\frac{\pi}{3}$

▶  $\frac{\pi}{4}$

▶  $\frac{\pi}{6}$

▶  $\frac{\pi}{2}$

Question No: 2 ( Marks: 1 ) - Please choose one

Let a function  $f$  be defined on an interval, and let  $x_1$  and  $x_2$  denotes two distinct points in that interval. If  $f(x_1) = f(x_2)$  for all points  $x_1$  and  $x_2$  then which of the following statement is correct?

- ▶  $f$  is a decreasing function
- ▶  $f$  is an increasing function
- ▶  $f$  is a constant function

**Question No: 3 ( Marks: 1 ) - Please choose one**

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Tan(x) is continuous every where except at points

- ▶  $\pm \frac{k\pi}{2} (k = 1, 3, 5, \dots)$
- ▶  $\pm \frac{k\pi}{2} (k = 2, 4, 6, \dots)$
- ▶  $\pm \frac{k\pi}{2} (k = 1, 2, 3, 4, 5, 6, \dots)$
- ▶

**Question No: 4 ( Marks: 1 ) - Please choose one**

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$\lim_{x \rightarrow \infty} (-2x) =$

- ▶ -2
- ▶ 0
- ▶ 2
- ▶ Does not exist

**Question No: 5 ( Marks: 1 ) - Please choose one**

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Suppose that  $f$  and  $g$  are differentiable functions of  $x$  then

$$\frac{d}{dx} [f][g] =$$

- ▶  $\frac{[f'] [g] - [f] [g']}{g^2}$
- ▶  $[f'] [g']$
- ▶  $[f'] [g] + [f] [g']$
- ▶  $[f'] [g] - [f] [g']$

**Question No: 6 ( Marks: 1 ) - Please choose one**

The solution set of the inequality  $|x+4| \geq 2$  is

- ▶  $(-\infty, -6] \cup [2, +\infty)$
- ▶ None of these
- ▶  $(-\infty, 6] \cup [-2, +\infty)$
- ▶  $(-\infty, -6] \cup [-2, +\infty)$

**Question No: 7 ( Marks: 1 ) - Please choose one**

A line is called a tangent line to the circle if it meets the circle at precisely .....

- ▶ One point
- ▶ Two points
- ▶ Infinite points

**Question No: 8 ( Marks: 1 ) - Please choose one**

Let a function  $f$  be defined on an interval, and let  $x_1$  and  $x_2$  denote points in that interval. If  $f(x_1) < f(x_2)$  whenever  $x_1 < x_2$  then which of the following statement is correct?

- ▶  $f$  is an increasing function.
- ▶  $f$  is a decreasing function.
- ▶  $f$  is a constant function.

**Question No: 9 ( Marks: 1 ) - Please choose one**

If  $f(x) = 3x^8 + 2x + 1$  then  $f'(x) =$  \_\_\_\_\_

- ▶  $3x^7 + 2$
- ▶  $24x^7 + 2$
- ▶  $3x^9 + 2x^2$

▶  $24x^9 + 2x^2$

**Question No: 10 ( Marks: 1 ) - Please choose one**

$\pi$  is a .....number

- ▶ Integer
- ▶ Rational
- ▶ **Irrational**
- ▶ Natural

**Question No: 11 ( Marks: 1 ) - Please choose one**

The set  $\{x: a \leq x \leq b\}$  can be written in the form of interval

- ▶ (a,b)
- ▶ (a,b]
- ▶ **[a,b]**

**Question No: 12 ( Marks: 1 ) - Please choose one**

Suppose that  $f$  and  $g$  are differentiable functions of  $x$  then

$$\frac{d}{dx} \left[ \frac{f}{g} \right] =$$

- ▶  **$\frac{[g][f'] - [f][g']}{g^2}$**
- ▶  $\frac{[g'] [f] - [f'] [g]}{g^2}$
- ▶  $\frac{[g][f'] - [f][g']}{f^2}$
- ▶  $\frac{[g'] [f] - [f'] [g]}{f^2}$

**Question No: 13 ( Marks: 1 ) - Please choose one**

The graph  $x = y^2$  is symmetric about -----axis

- ▶ X-axis
- ▶ Y-axis
- ▶ Origin

**Question No: 14 ( Marks: 1 ) - Please choose one**

$$\lim_{x \rightarrow -7} \frac{x^2 - 49}{x + 7}$$

- ▶ -14
- ▶ 0
- ▶  $\infty$
- ▶ Limit does not exist

**Question No: 15 ( Marks: 1 ) - Please choose one**

Chain rule is a rule for differentiating \_\_\_\_\_ of functions.

- ▶ Product
- ▶ Sum
- ▶ Difference
- ▶ Composition

**Question No: 16 ( Marks: 1 ) - Please choose one**

$$\lim_{x \rightarrow a} f(x) = \dots \text{where } f(x) = k$$

The \_\_\_\_\_ (k is a constant)

- ▶ k+2
- ▶ k+1
- ▶ k

**Question No: 17 ( Marks: 1 ) - Please choose one**

For any number  $\epsilon > 0$  if we can find an open interval  $(x_0, x_1)$  on the x-axis containing the point "a" such that  $L - \epsilon < f(x) < L + \epsilon$  for each x in  $(x_0, x_1)$  except the possible x = a then we say  $\lim_{x \rightarrow a} f(x) =$  \_\_\_\_\_

- ▶ L

- ▶  $L - \varepsilon$
- ▶  $L + \varepsilon$
- ▶  $L + 1$

**Question No: 18 ( Marks: 1 ) - Please choose one**

If  $2x - y = -3$  then  $\frac{dy}{dx} =$

- ▶ 2
- ▶ -2
- ▶ 0
- ▶ -3

**Question No: 19 ( Marks: 1 ) - Please choose one**

The graph of the equation  $y = x^2 - 4x + 5$  will represent

- ▶ Parabola
- ▶ Straight line
- ▶ Two straight lines
- ▶ Ellipse

**Question No: 20 ( Marks: 1 ) - Please choose one**

The equation of line of the form  $y - y_1 = m(x - x_1)$  is known as

- ▶ Point-slope form
- ▶ Two points form
- ▶ Intercepts form
- ▶ Slope intercept form

**Question No: 21 ( Marks: 2 )**

If  $y = 5 \cos(x^2 + 1)$  Find  $dy/dx$  by using "The chain rule".

**Question No: 22 ( Marks: 2 )**

Prove that  $\lim_{x \rightarrow 1} (x+5) = 6$ , using the definition of limit.

**Question No: 23 ( Marks: 3 )**

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Find an equation of the tangent line to the curve

$$y = \frac{2}{x^2 + x}$$

at the point where  $x = 1$

**Question No: 24 ( Marks: 3 )**

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$$\lim_{x \rightarrow 0} \frac{\sin(5x)}{3x}$$

Compute

**Question No: 25 ( Marks: 5 )**

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$$f(x) = x^4 - 4x^3 + 4x^2$$

Find all critical points of

**Question No: 26 ( Marks: 5 )**

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$$\frac{dy}{dx} \quad y = x^2(\cot x) - \frac{1}{x^2}$$

Find if

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